



University of Kerala

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|----------------|---|---------------------|----------------------|-----------------------|-------------------------|
| Discipline | Mathematics | | | | |
| Course Code | UK2MDCMAT103 | | | | |
| Course Title | Introduction to Modular Arithmetic and Cryptography | | | | |
| Type of Course | MDC | | | | |
| Semester | II | | | | |
| Academic Level | 100-199 | | | | |
| Course Details | Credit | Lecture per week | Tutorial per week | Practical per week | Total Hours per week |
| | 3 | 3 | | | 3 |
| Pre-requisites | Basic properties of integers, divisibility, gcd Linear Diophantine equations, Unique factorization | | | | |
| Course Summary | This is a short introduction to Cryptography using congruences. | | | | |

Detailed Syllabus

| Module | Unit | Contents | Hrs |
|------------|------|--|----------|
| I | | Modular Arithmetic | 9 |
| | 1 | Definition of congruence relation, Modular exponentiation, Divisibility tests, linear congruences, (Chapter 5: Sections 5.1, 5.2, 5.3, 5.4 of Text[1]) | |
| II | | Three Classical Theorems | 9 |
| | 2 | The Chinese remainder theorem, Fermat's theorem, Euler's theorem (Chapter 5: Sections 5.5, Chapter 6: Section 6.1, 6.2 of Text[1]) | |
| III | | Introduction to Cryptography | 9 |
| | 3 | Shift and affine cipher, Vigenere ciphers, transposition ciphers (Chapter 7: Sections 7.1, 7.2, 7.3, 7.4 of Text[1]) | |

| Module | Unit | Contents | Hrs |
|-----------|---|---|----------|
| IV | RSA and applications | | 9 |
| | 4 | RSA, stream ciphers (Chapter 7: Sections 7.5, 7.6 of Text[1]) | |
| V | Suggestions for the teacher designed module | | 9 |
| | For internal assessment examinations only. | | |
| | 5 | Wilson's theorem, Block ciphers, Secret sharing | |
| | These topics can be found on Chapters 6 and 7 of Text [1] | | |

Textbook

1. James S.Kraft, Lawrence C. Washington. Elementary Number Theory, CRC Press, 2015.

References

1. James S.Kraft, Lawrence C. Washington, An Introduction to Number Theory with Cryptography, CRC Press, 2014.
2. G A Jones, J M Jones, Elementary Number Theory, Springer, 1998.
3. Thomas Koshy, Elementary Number Theory with Applications, 2nd Edition, Academic Press, 2007.

Course Outcomes

| CO No. | Upon completion of the course the graduate will be able to | PO/PSO | Cognitive Level | Knowledge Category | Lecture(L) Tutorial (T) | Assignment (As) |
|--------|---|------------|-----------------|--------------------|----------------------------|-----------------|
| CO 1 | Describe the basic concept of Modular arithmetic | PSO1, PSO2 | R | F,C | L | |
| CO 2 | Apply congruence to solve various problems. | PSO3 | U,Ap | P | L | |
| CO 3 | Analyse the properties of integers using congruences via three milestone theorems | PSO3, PSO4 | U,An | C | L | |
| CO 4 | Apply congruence to cryptography | PSO3 | R,U,An | C | L | |

(R-Remember, U-Understand, Ap-Apply, An-Analyse, E-Evaluate, C-Create)
(F-Factual, C-Conceptual, P-Procedural, M-Metacognitive)

Mapping of CO with PSOs and POs

| | PSO1 | PSO2 | PSO3 | PSO4 | PSO5 | PSO6 | PO1 | PO2 | PO3 | PO4 | PO5 | PO6 | PO7 | PO8 |
|-----|------|------|------|------|------|------|-----|-----|-----|-----|-----|-----|-----|-----|
| CO1 | 2 | 1 | - | - | - | - | - | - | - | - | - | - | - | - |
| CO2 | - | - | 3 | - | - | - | - | - | - | - | - | - | - | - |
| CO3 | - | - | 1 | 2 | - | - | - | - | - | - | - | - | - | - |
| CO4 | - | - | 3 | - | - | - | - | - | - | - | - | - | - | - |

(- -Nil, 1-Slightly/Low, 2-Moderate/Medium, 3-Substantial/High)

Assessment Rubrics

- Quiz/Assignment/Discussion/Seminar
- Midterm Exam
- Programming Assignments
- Final Exam

Mapping of COs to Assessment Rubrics

| | Internal Examination | Assignment | Project Evaluation | End Semester Exam |
|-----|----------------------|------------|--------------------|-------------------|
| CO1 | ✓ | | | ✓ |
| CO2 | ✓ | ✓ | | ✓ |
| CO3 | ✓ | | | ✓ |
| CO4 | | ✓ | | ✓ |